

34.5 A storage tank contains $250^\circ F$ air at 100psia . The air is released and expanded through a 86% efficient turbine to 15psia . What is the specific work produced by the turbine? Assume air behaves as an ideal gas.

- A. $61 \frac{\text{Btu}}{\text{lb}}$
- B. $90 \frac{\text{Btu}}{\text{lb}}$
- C. $124 \frac{\text{Btu}}{\text{lb}}$
- D. $142 \frac{\text{Btu}}{\text{lb}}$

Consider the pressurized air entering the turbine as State 1 and the air exiting the turbine as State 2. Use the **Air at Low Pressure** table to obtain the enthalpy and relative pressure at State 1. Notice that for air these parameters are a function of temperature only.

$$T_1 = 250^\circ F$$

$$P_1 = 100\text{psia}$$

$$h_1 = 170 \frac{\text{Btu}}{\text{lb}}$$

$$P_{r,1} = 3.623$$

Set up a proportion and use the actual pressures at State 1 and State 2 along with the relative pressure at State 1 to determine the relative pressure at State 2.

$$\frac{P_{r,1}}{P_{r,2}} = \frac{P_1}{P_2}$$

$$P_{r,2} = P_{r,1} \left(\frac{P_2}{P_1} \right) = 3.623 \left(\frac{15\text{psia}}{100\text{psia}} \right) = 0.543$$

Use the air table again to obtain the *ideal* enthalpy corresponding to the relative pressure at State 2.

$$h_2 = 98.6 \frac{\text{Btu}}{\text{lb}}$$

To find the *actual* specific work for the turbine, take the difference between the entering and exiting enthalpies and multiply by the turbine efficiency.

$$w = \eta (h_1 - h_2) = (0.86) \left(170 \frac{\text{Btu}}{\text{lb}} - 98.6 \frac{\text{Btu}}{\text{lb}} \right) = 61.4 \frac{\text{Btu}}{\text{lb}}$$

Answer A